### Discontinuity, Nonlinearity, and Complexity

#### **Editors**

#### Valentin Afraimovich

San Luis Potosi University, IICO-UASLP, Av.Karakorum 1470 Lomas 4a Seccion, San Luis Potosi, SLP 78210, Mexico

Fax: +52 444 825 0198

Email: valentin@cactus.iico.uaslp.mx

#### Xavier Leoncini

Centre de Physique Théorique, Aix-Marseille Université, CPT Campus de Luminy, Case 907 13288 Marseille Cedex 9, France

Fax: +33 4 91 26 95 53

Email: leoncini@cpt.univ-mrs.fr

Fax: +1 303 497 5862

**Dimitry Volchenkov** 

Email: Lev.A.Ostrovsky@noaa.gov

Lev Ostrovsky

The Center of Excellence Cognitive Interaction Technology Universität Bielefeld, Mathematische Physik Universitätsstraße 25 D-33615 Bielefeld, Germany

Zel Technologies/NOAA ESRL, Boulder CO 80305, USA

Fax: +49 521 106 6455

Email: volchenk@physik.uni-bielefeld.de

#### **Associate Editors**

#### **Marat Akhmet**

Department of Mathematics Middle East Technical University 06531 Ankara, Turkey Fax: +90 312 210 2972 Email: marat@metu.edu.tr

#### Dumitru Baleanu

Department of Mathematics and Computer Sciences Cankaya University, Balgat 06530 Ankara, Turkey Email: dumitru@cankaya.edu.tr

#### Marian Gidea

Department of Mathematics Northeastern Illinois University Chicago, IL 60625, USA Fax: +1 773 442 5770 Email: mgidea@neiu.edu

#### Juan Luis García Guirao

Department of Applied Mathematics Technical University of Cartagena Hospital de Marina 30203-Cartagena, SPAIN

Fax:+34 968 325694 E-mail: juan.garcia@upct.es

#### Ranis N. Ibragimov

Applied Statistics Lab GE Global Research 1 Research Circle, K1-4A64 Niskayuna, NY 12309 Email: ibrranis@gmail.com

#### Nikolai A. Kudryashov

Department of Applied Mathematics Moscow Engineering and Physics Institute (State University), 31 Kashirskoe Shosse 115409 Moscow, Russia Fax: +7 495 324 11 81

Fax: +/ 495 324 11 81 Email: kudryashov@mephi.ru

#### Gennady A. Leonov

Department of Mathematics and Mechanics St-Petersburg State University 198504, Russia

Email: leonov@math.spbu.ru

#### E.N. Macau

Lab. Associado de Computção e Mateática Aplicada, Instituto Nacional de Pesquisas Espaciais, Av. dos Astronautas, 1758 12227-010 Sáo José dos Campos –SP Brazil Email: elbert@lac.inpe.br

#### Jose Antonio Tenreiro Machado

ISEP-Institute of Engineering of Porto Dept. of Electrotechnical Engineering Rua Dr. Antonio Bernardino de Almeida 4200-072 Porto, Portugal

Fax: +351 22 8321159 Email: jtm@dee.isep.ipp.pt

#### **Denis Makarov**

Pacific Oceanological Institute of the Russian Academy of Sciences,43 Baltiiskaya St., 690041 Vladivostok, RUSSIA

Tel/fax: 007-4232-312602. Email: makarov@poi.dvo.ru

#### Josep J. Masdemont

Department of Matematica Aplicada I Universitat Politecnica de Catalunya (UPC) Diagonal 647 ETSEIB 08028 Barcelona, Spain Email: josep@barquins.upc.edu

#### Michael A. Zaks

Technische Universität Berlin DFG-Forschungszentrum Matheon -Mathematics for key technologies Sekretariat MA 3-1, Straße des 17. Juni 136

10623 Berlin

Email: zaks@physik.hu-berlin.de

#### **Editorial Board**

#### Vadim S. Anishchenko

Department of Physics Saratov State University Astrakhanskaya 83, 410026, Saratov, Russia

Fax: (845-2)-51-4549 Email: wadim@info.sgu.ru

#### Mokhtar Adda-Bedia

Laboratoire de Physique Statistique Ecole Normale Supérieure 24 rue Lhomond, 75231 Paris Cedex 05 France

Fax: +33 1 44 32 34 33 Email: adda@lps.ens.fr

#### Ravi P. Agarwal

Department of Mathematics Texas A&M University – Kingsville, Kingsville, TX 78363-8202 USA

Email: agarwal@tamuk.edu

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Editors
Valentin Afraimovich
Xavier Leoncini
Lev Ostrovsky
Dimitry Volchenkov



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The interdisciplinary journal publishes original and new results on recent developments, discoveries and progresses on Discontinuity, Nonlinearity and Complexity in physical and social sciences. The aim of the journal is to stimulate more research interest for exploration of discontinuity, complexity, nonlinearity and chaos in complex systems. The manuscripts in dynamical systems with nonlinearity and chaos are solicited, which includes mathematical theories and methods, physical principles and laws, and computational techniques. The journal provides a place to researchers for the rapid exchange of ideas and techniques in discontinuity, complexity, nonlinearity and chaos in physical and social sciences. Topics of interest include but not limited to

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- Nonlinear discrete systems and symbolic dynamics
- · Fractional dynamical systems and control
- · Stochastic dynamical systems and randomness
- Complexity, self-similarity and synchronization
- Complex nonlinear phenomena in physical systems
- · Stability, bifurcation and chaos in complex systems
- · Turbulence and other complex phenomena in hydrodynamics
- · Nonlinear waves and solitons
- · Dynamical networks
- · Combinatorial aspects of dynamical systems
- Biological dynamics and biophysics
- Pattern formation, social science and complexization

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#### Igor Belykh

Department of Mathematics & Statistics Georgia State University 30 Pryor Street, Atlanta, GA 30303-3083

Email: ibelykh@gsu.edu

#### Didier Bénisti

CEA, DAM, DIF 91297 Arpajon Cedex France

Fax: +33 169 267 106 Email: didier.benisti@cea.fr

#### Alexandre N. Carvalho

Departamento de Matem'atica, Instituto de Ci^encias Matem'aticas e de Computa,c^ao Universidade de S^ao Paulo - Campus de S^ao Carlos, Caixa Postal 668, 13560-970 S^ao Carlos SP, Brazil

Email: andcarva@icmc.usp.br

#### Maurice Courbage

CNRS-UMR 7057 "Matière et Systèmes Complexes", 75205 Paris Cedex 13 France Email: maurice.courbage@univ-parisdiderot.fr

#### Michal Feckan

Department of Mathematical Analysis and Numerical Mathematics, Comenius University Mlynska dolina 842 48 Bratislava, Slovakia Fax: +421 2 654 12 305

Email: michal.feckan@fmph.uniba.sk

#### **Marie-Christine Firpo**

Laboratoire de Physique des Plasmas CNRS UMR 7648, Ecole Polytechnique 91128 Palaiseau cedex, France Tel: (00 33) 1 69 33 59 04 Fax: (00 33) 1 69 33 59 06

E-mail:

marie-christine.firpo@lpp.polytechnique.fr

#### Stefano Galatolo

Dipartimento di Matematica Applicata Via Buonattoti 1 56127 Pisa, Italy

Email: s.galatolo@ing.unipi.it

#### N.H. Ibragimov

Department of Mathematics, IHN Blekinge Institute of Technology S-371 79 Karlskrona, Sweden Fax: +46 455 385 407

Email: nail.ibragimov@bth.se

#### Tassilo Küpper

Mathematical Institute University of Cologne, Weyertal 86-90 D-50931 Cologne, Germany Fax: +49 221 470 5021

Email: kuepper@math.uni-koeln.de

#### Marc Leonetti

IRPHE, Aix-Marseille Université UMR CNRS 6594, Technopôle de Château-Gombert 13384 Marseilles Cedex 13 France

Fax: + 33 4 13 55 20 01 Email: <u>leonetti@irphe.univ-mrs.fr</u>

#### Yuri Maistrenko

Institute of Mathematics National Academy of Sciences of Ukraine Volodymyrska Str. 54, room 232 01030 Kiev, Ukraine

E-mail: y.maistrenko@biomed.kiev.ua

#### Mikhail Malkin

Department of Mathematics and Mechanics Nizhny Novgorod State University, Nizhny Novgorod, Russia

Fax: +7 831 465 76 01 Email: <u>malkin@unn.ru</u>

#### Vladimir I. Nekorkin

Institute of Applied Physics of RAS 46 Ul'yanov Street, 603950, Nizhny Novgorod, Russia

Email: vnekorkin@neuron.appl.sci-nnov.ru

#### **Dmitry E. Pelinovsky**

Department of Mathematics & Statistics McMaster University, 1280 Main Street West, Hamilton, Ontario, Canada L8S 4K1

Fax: +1 905 522 0935

Email: dmpeli@math.mcmaster.ca

#### Alexander N. Pisarchik

Centro de Investigaciones en Optica A.C. Loma del Bosque #115 Lomas del Campes-tre 37150 Leon Guanajuato, Mexico Fax: +52 477 441 4209 Email: apisarch@cio.mx

#### Raul Rechtman

Centro de Investigacion en Energia Universidad Nacional Autonoma de Mexico Priv. Xochicalco S/N, Temixco Morelos 62580, Mexico

Fax: +52 555 622 9791 Email: rrs@cie.unam.mx

#### Nikolai Rulkov

BioCircuits Institute, University of California, San Diego, 9500 Gilman Drive #0328 La Jolla, CA 92093-0328, USA Fax: (858) 534-1892

Email: nrulkov@ucsd.edu

#### **Andrey Shilnikov**

Department of Mathematics and Statistics Georgia State University, 100 Piedmont Ave SE Atlanta GA 30303, USA Fax: +1 404 413 6403

Email: ashilnikov@gsu.edu

#### Vasily E. Tarasov

Skobeltsyn Institute of Nuclear Physics Moscow State University 119992 Moscow, Russia Fax: +7 495 939 03 97

Email: tarasov@theory.sinp.msu.ru

#### Marco Thiel

Institute for Mathematical Biology and Complex Systems University of Aberdeen AB243UE Aberdeen, Scotland, UK

Fax: +44 1224 273105 Email: m.thiel@abdn.ac.uk

#### Vladimir V. Uchaikin

Ulyanovsk State University L.Tolstoy Str. 42 Ulyanovsk 432700, Russia Fax: +7 842 232 90 14 Email: vuchaikin@gmail.com

#### Edgardo Ugalde

Instituto de Fisica Universidad Autonoma de San Luis Potosi Av. Manuel Nava 6, Zona Universitaria San Luis Potosi SLP CP 78290, Mexico

Email: gallo.ugalde@gmail.com

#### Alexei A. Vasiliev

Space Research Institute Profsoyuznaya 84/32 Moscow 117997, Russia Fax: +7 495 333 12 48 Email: valex@iki.rssi.ru

#### **Todd Young**

Department of Mathematics Ohio University Athens, OH 45701, USA Email: young@math.ohiou.edu